

Forecasting

BUS 735: Business Decision Making and Research

Goals and Agenda

2 / 14

Learning Objective

Learn how to identify regularities in time series data

Learn popular univariate time series forecasting methods

Practice what we learn.

More practice.

Assess what we have learned

Active Learning Activity

Lecture / Excel Example.

Lecture / Excel Example.

In-class exercise.

Read Chapter 15, Homework exercises.

Quiz??

Working with Example Data

3/ 14

- Dataset: Total number of Mining, Logging, and Construction employees (in thousands) in the La Crosse area (obtained from Bureau of Labor Statistics website, <http://www.bls.gov>).
- To plot the data, we need to convert it to a single column:
 - 1 First generate observation numbers 1 through 284
 - 2 Figure out what row the observation is in:
`=int((obs-1)/12)+1`
 - 3 Figure out what column the observation is in:
`=mod((obs-1),12)+1`
 - 4 Pick out the right observation:
`=offset([top_corner],row,col)`
- Create dates: 1990.0 through 2013.58.

Graphing Example Data

- In Excel: Insert, Line, Line with markers.
- Right click on data, select Select Data.
- Remove all the nonsense there.
- Select Add.
- Type "Employment" in Series Name. Select data for Series Values.
- Click Edit under Horizontal Axis Values.
- Select dates.

Time Series Characteristics

- **Trend:** gradual, long-term movement of the data in a positive or negative direction.
- **Cycle:** repetitive up-and-down movement of the data, each “cycle” need not be the same length or magnitude.
- **Seasonal pattern:** up-and-down movement of the data that can be predicted quite accurately by the time of the year.
- **Random variations:** movements in the data that are otherwise unpredictable.

Time Series Characteristics

- **Trend:** gradual, long-term movement of the data in a positive or negative direction.
- **Cycle:** repetitive up-and-down movement of the data, each “cycle” need not be the same length or magnitude.
- **Seasonal pattern:** up-and-down movement of the data that can be predicted quite accurately by the time of the year.
- **Random variations:** movements in the data that are otherwise unpredictable.

Time Series Characteristics

- **Trend:** gradual, long-term movement of the data in a positive or negative direction.
- **Cycle:** repetitive up-and-down movement of the data, each “cycle” need not be the same length or magnitude.
- **Seasonal pattern:** up-and-down movement of the data that can be predicted quite accurately by the time of the year.
- **Random variations:** movements in the data that are otherwise unpredictable.

Time Series Characteristics

- **Trend:** gradual, long-term movement of the data in a positive or negative direction.
- **Cycle:** repetitive up-and-down movement of the data, each “cycle” need not be the same length or magnitude.
- **Seasonal pattern:** up-and-down movement of the data that can be predicted quite accurately by the time of the year.
- **Random variations:** movements in the data that are otherwise unpredictable.

Time Series Analysis

6/ 14

- **Time series analysis:** use of statistical methods to uncover trend, cyclical patterns, and seasonal patterns; and using this information to forecast future outcomes for a variable.
- **Univariate time series:** using many observations of only the variable of interest to forecast that variable.
- **Multivariate time series:** using one or more related variables to help forecast variable of interest.
 - New housing sales may also help predict construction employment.
 - National price measures for costs of building materials may also help predict construction employment.
- BUS 735: Focus on univariate time series analysis.

Time Series Analysis

6/ 14

- **Time series analysis:** use of statistical methods to uncover trend, cyclical patterns, and seasonal patterns; and using this information to forecast future outcomes for a variable.
- **Univariate time series:** using many observations of only the variable of interest to forecast that variable.
- **Multivariate time series:** using one or more related variables to help forecast variable of interest.
 - New housing sales may also help predict construction employment.
 - National price measures for costs of building materials may also help predict construction employment.
- BUS 735: Focus on univariate time series analysis.

Time Series Analysis

6/ 14

- **Time series analysis:** use of statistical methods to uncover trend, cyclical patterns, and seasonal patterns; and using this information to forecast future outcomes for a variable.
- **Univariate time series:** using many observations of only the variable of interest to forecast that variable.
- **Multivariate time series:** using one or more related variables to help forecast variable of interest.
 - New housing sales may also help predict construction employment.
 - National price measures for costs of building materials may also help predict construction employment.
- BUS 735: Focus on univariate time series analysis.

Time Series Analysis

6 / 14

- **Time series analysis:** use of statistical methods to uncover trend, cyclical patterns, and seasonal patterns; and using this information to forecast future outcomes for a variable.
- **Univariate time series:** using many observations of only the variable of interest to forecast that variable.
- **Multivariate time series:** using one or more related variables to help forecast variable of interest.
 - New housing sales may also help predict construction employment.
 - National price measures for costs of building materials may also help predict construction employment.
- BUS 735: Focus on univariate time series analysis.

Time Series Analysis

6/ 14

- **Time series analysis:** use of statistical methods to uncover trend, cyclical patterns, and seasonal patterns; and using this information to forecast future outcomes for a variable.
- **Univariate time series:** using many observations of only the variable of interest to forecast that variable.
- **Multivariate time series:** using one or more related variables to help forecast variable of interest.
 - New housing sales may also help predict construction employment.
 - National price measures for costs of building materials may also help predict construction employment.
- BUS 735: Focus on univariate time series analysis.

Time Series Analysis

6/ 14

- **Time series analysis:** use of statistical methods to uncover trend, cyclical patterns, and seasonal patterns; and using this information to forecast future outcomes for a variable.
- **Univariate time series:** using many observations of only the variable of interest to forecast that variable.
- **Multivariate time series:** using one or more related variables to help forecast variable of interest.
 - New housing sales may also help predict construction employment.
 - National price measures for costs of building materials may also help predict construction employment.
- BUS 735: Focus on univariate time series analysis.

Moving Average

7 / 14

- **Naïve forecast:** Forecast for tomorrow is what happened today.
 - Often used to measure usefulness of other time series forecasts.
- **Moving average:** uses several recent values to forecast the next period's outcome.

$$MA_{t,q} = \frac{1}{q} \sum_{i=1}^q x_{t-i}$$

- x_t denotes the value of the variable at time t ,
- $MA_{t,q}$ denotes the Moving Average forecast for time t , using the most recent q periods.

Moving Average

7/ 14

- **Naïve forecast:** Forecast for tomorrow is what happened today.
 - Often used to measure usefulness of other time series forecasts.
- **Moving average:** uses several recent values to forecast the next period's outcome.

$$MA_{t,q} = \frac{1}{q} \sum_{i=1}^q x_{t-i}$$

- x_t denotes the value of the variable at time t ,
- $MA_{t,q}$ denotes the Moving Average forecast for time t , using the most recent q periods.

Moving Average

7 / 14

- **Naïve forecast:** Forecast for tomorrow is what happened today.
 - Often used to measure usefulness of other time series forecasts.
- **Moving average:** uses several recent values to forecast the next period's outcome.

$$MA_{t,q} = \frac{1}{q} \sum_{i=1}^q x_{t-i}$$

- x_t denotes the value of the variable at time t ,
- $MA_{t,q}$ denotes the Moving Average forecast for time t , using the most recent q periods.

Moving Average

7 / 14

- **Naïve forecast:** Forecast for tomorrow is what happened today.
 - Often used to measure usefulness of other time series forecasts.
- **Moving average:** uses several recent values to forecast the next period's outcome.

$$MA_{t,q} = \frac{1}{q} \sum_{i=1}^q x_{t-i}$$

- x_t denotes the value of the variable at time t ,
- $MA_{t,q}$ denotes the Moving Average forecast for time t , using the most recent q periods.

Moving Average

7 / 14

- **Naïve forecast:** Forecast for tomorrow is what happened today.
 - Often used to measure usefulness of other time series forecasts.
- **Moving average:** uses several recent values to forecast the next period's outcome.

$$MA_{t,q} = \frac{1}{q} \sum_{i=1}^q x_{t-i}$$

- x_t denotes the value of the variable at time t ,
- $MA_{t,q}$ denotes the Moving Average forecast for time t , using the most recent q periods.

Moving Average

7 / 14

- **Naïve forecast:** Forecast for tomorrow is what happened today.
 - Often used to measure usefulness of other time series forecasts.
- **Moving average:** uses several recent values to forecast the next period's outcome.

$$MA_{t,q} = \frac{1}{q} \sum_{i=1}^q x_{t-i}$$

- x_t denotes the value of the variable at time t ,
- $MA_{t,q}$ denotes the Moving Average forecast for time t , using the most recent q periods.

Moving Average Properties

8 / 14

- Moving average lag length:
 - Longer lag lengths cause forecast to react more quickly/slowly to recent changes in the variable.
 - Longer lag lengths cause forecast to be more smooth/volatile.
- Performs (forecasting accuracy) best with data that has
 - No pronounced cyclical or seasonal variation.
 - No long-term trend.

Moving Average Properties

8 / 14

- Moving average lag length:
 - Longer lag lengths cause forecast to react more quickly/slowly to recent changes in the variable.
 - Longer lag lengths cause forecast to be more smooth/volatile.
- Performs (forecasting accuracy) best with data that has
 - No pronounced cyclical or seasonal variation.
 - No long-term trend.

Moving Average Properties

8 / 14

- Moving average lag length:
 - Longer lag lengths cause forecast to react more quickly/slowly to recent changes in the variable.
 - Longer lag lengths cause forecast to be more smooth/volatile.
- Performs (forecasting accuracy) best with data that has
 - No pronounced cyclical or seasonal variation.
 - No long-term trend.

Moving Average Properties

8 / 14

- Moving average lag length:
 - Longer lag lengths cause forecast to react more quickly/slowly to recent changes in the variable.
 - Longer lag lengths cause forecast to be more smooth/volatile.
- Performs (forecasting accuracy) best with data that has
 - No pronounced cyclical or seasonal variation.
 - No long-term trend.

Moving Average Properties

8 / 14

- Moving average lag length:
 - Longer lag lengths cause forecast to react more quickly/slowly to recent changes in the variable.
 - Longer lag lengths cause forecast to be more smooth/volatile.
- Performs (forecasting accuracy) best with data that has
 - No pronounced cyclical or seasonal variation.
 - No long-term trend.

Moving Average Properties

8 / 14

- Moving average lag length:
 - Longer lag lengths cause forecast to react more quickly/slowly to recent changes in the variable.
 - Longer lag lengths cause forecast to be more smooth/volatile.
- Performs (forecasting accuracy) best with data that has
 - No pronounced cyclical or seasonal variation.
 - No long-term trend.

Weighted Moving Average

9 / 14

- **Weighted moving average:** like a moving average, but larger weights are assigned to more recent observations.

$$WMA_{t,q} = \sum_{i=1}^q w_i x_{t-i}$$

- w_i is the weight given to the observation that occurred i periods ago.
- $\sum_{i=1}^q w_i = 1$
- Typically, $w_i > w_{i+1}$.
- More recent observations are viewed as more informative.

Weighted Moving Average

- **Weighted moving average:** like a moving average, but larger weights are assigned to more recent observations.

$$WMA_{t,q} = \sum_{i=1}^q w_i x_{t-i}$$

- w_i is the weight given to the observation that occurred i periods ago.
- $\sum_{i=1}^q w_i = 1$
- Typically, $w_i > w_{i+1}$.
- More recent observations are viewed as more informative.

Weighted Moving Average

- **Weighted moving average:** like a moving average, but larger weights are assigned to more recent observations.

$$WMA_{t,q} = \sum_{i=1}^q w_i x_{t-i}$$

- w_i is the weight given to the observation that occurred i periods ago.
- $\sum_{i=1}^q w_i = 1$
- Typically, $w_i > w_{i+1}$.
- More recent observations are viewed as more informative.

Weighted Moving Average

- **Weighted moving average:** like a moving average, but larger weights are assigned to more recent observations.

$$WMA_{t,q} = \sum_{i=1}^q w_i x_{t-i}$$

- w_i is the weight given to the observation that occurred i periods ago.
- $\sum_{i=1}^q w_i = 1$
- Typically, $w_i > w_{i+1}$.
- More recent observations are viewed as more informative.

Weighted Moving Average

- **Weighted moving average:** like a moving average, but larger weights are assigned to more recent observations.

$$WMA_{t,q} = \sum_{i=1}^q w_i x_{t-i}$$

- w_i is the weight given to the observation that occurred i periods ago.
 - $\sum_{i=1}^q w_i = 1$
 - Typically, $w_i > w_{i+1}$.
- More recent observations are viewed as more informative.

Weighted Moving Average

- **Weighted moving average:** like a moving average, but larger weights are assigned to more recent observations.

$$WMA_{t,q} = \sum_{i=1}^q w_i x_{t-i}$$

- w_i is the weight given to the observation that occurred i periods ago.
- $\sum_{i=1}^q w_i = 1$
- Typically, $w_i > w_{i+1}$.
- More recent observations are viewed as more informative.

Exponential Smoothing

- **Exponential smoothing:** Averaging method using all previous data, but puts weights larger weight on the more recent observations.

$$F_t = \alpha x_{t-1} + (1 - \alpha)F_{t-1}$$

- F_t is the forecast for period t .
- x_{t-1} is the value of the variable in the previous time period, $t - 1$.
- Useful for capturing information on recent seasonal or cyclical patterns (but with a lag).
- $\alpha \in [0, 1]$ is the smoothing parameter.
 - When α is larger, more weight is given to most recent observations.

Exponential Smoothing

- **Exponential smoothing:** Averaging method using all previous data, but puts weights larger weight on the more recent observations.

$$F_t = \alpha x_{t-1} + (1 - \alpha)F_{t-1}$$

- F_t is the forecast for period t .
- x_{t-1} is the value of the variable in the previous time period, $t - 1$.
- Useful for capturing information on recent seasonal or cyclical patterns (but with a lag).
- $\alpha \in [0, 1]$ is the smoothing parameter.
 - When α is larger, more weight is given to most recent observations.

Exponential Smoothing

- **Exponential smoothing:** Averaging method using all previous data, but puts weights larger weight on the more recent observations.

$$F_t = \alpha x_{t-1} + (1 - \alpha)F_{t-1}$$

- F_t is the forecast for period t .
- x_{t-1} is the value of the variable in the previous time period, $t - 1$.
- Useful for capturing information on recent seasonal or cyclical patterns (but with a lag).
- $\alpha \in [0, 1]$ is the smoothing parameter.
 - When α is larger, more weight is given to most recent observations.

Exponential Smoothing

- **Exponential smoothing:** Averaging method using all previous data, but puts weights larger weight on the more recent observations.

$$F_t = \alpha x_{t-1} + (1 - \alpha)F_{t-1}$$

- F_t is the forecast for period t .
- x_{t-1} is the value of the variable in the previous time period, $t - 1$.
- Useful for capturing information on recent seasonal or cyclical patterns (but with a lag).
- $\alpha \in [0, 1]$ is the smoothing parameter.
 - When α is larger, more weight is given to most recent observations.

Exponential Smoothing

- **Exponential smoothing:** Averaging method using all previous data, but puts weights larger weight on the more recent observations.

$$F_t = \alpha x_{t-1} + (1 - \alpha)F_{t-1}$$

- F_t is the forecast for period t .
- x_{t-1} is the value of the variable in the previous time period, $t - 1$.
- Useful for capturing information on recent seasonal or cyclical patterns (but with a lag).
- $\alpha \in [0, 1]$ is the smoothing parameter.
 - When α is larger, more weight is given to most recent observations.

Exponential Smoothing

- **Exponential smoothing:** Averaging method using all previous data, but puts weights larger weight on the more recent observations.

$$F_t = \alpha x_{t-1} + (1 - \alpha)F_{t-1}$$

- F_t is the forecast for period t .
- x_{t-1} is the value of the variable in the previous time period, $t - 1$.
- Useful for capturing information on recent seasonal or cyclical patterns (but with a lag).
- $\alpha \in [0, 1]$ is the smoothing parameter.
 - When α is larger, more weight is given to most recent observations.

Exponential Smoothing

- **Exponential smoothing:** Averaging method using all previous data, but puts weights larger weight on the more recent observations.

$$F_t = \alpha x_{t-1} + (1 - \alpha)F_{t-1}$$

- F_t is the forecast for period t .
- x_{t-1} is the value of the variable in the previous time period, $t - 1$.
- Useful for capturing information on recent seasonal or cyclical patterns (but with a lag).
- $\alpha \in [0, 1]$ is the smoothing parameter.
 - When α is larger, more weight is given to most recent observations.

Adjusted Exponential Smoothing

11/ 14

- **Adjusted exponential smoothing:** exponential smoothing that is adjusted to incorporate information on a *long-term trend*.

$$AF_t = F_t + T_t$$

- AF_t is the adjusted exponential smoothing forecast.
 - F_t is the regular exponential smoothing forecast.
 - T_t is the latest estimate of the trend.
- Trend is computed by,

$$T_t = \beta(F_t - F_{t-1}) + (1 - \beta)T_{t-1}$$

- $\beta \in [0, 1]$ is a trend weighting parameter.
- Trend formula allows for changing trend throughout the data.

Adjusted Exponential Smoothing

11/ 14

- **Adjusted exponential smoothing:** exponential smoothing that is adjusted to incorporate information on a *long-term trend*.

$$AF_t = F_t + T_t$$

- AF_t is the adjusted exponential smoothing forecast.
- F_t is the regular exponential smoothing forecast.
- T_t is the latest estimate of the trend.
- Trend is computed by,

$$T_t = \beta(F_t - F_{t-1}) + (1 - \beta)T_{t-1}$$

- $\beta \in [0, 1]$ is a trend weighting parameter.
- Trend formula allows for changing trend throughout the data.

Adjusted Exponential Smoothing

11/ 14

- **Adjusted exponential smoothing:** exponential smoothing that is adjusted to incorporate information on a *long-term trend*.

$$AF_t = F_t + T_t$$

- AF_t is the adjusted exponential smoothing forecast.
- F_t is the regular exponential smoothing forecast.
- T_t is the latest estimate of the trend.
- Trend is computed by,

$$T_t = \beta(F_t - F_{t-1}) + (1 - \beta)T_{t-1}$$

- $\beta \in [0, 1]$ is a trend weighting parameter.
- Trend formula allows for changing trend throughout the data.

Adjusted Exponential Smoothing

11/ 14

- **Adjusted exponential smoothing:** exponential smoothing that is adjusted to incorporate information on a *long-term trend*.

$$AF_t = F_t + T_t$$

- AF_t is the adjusted exponential smoothing forecast.
- F_t is the regular exponential smoothing forecast.
- T_t is the latest estimate of the trend.
- Trend is computed by,

$$T_t = \beta(F_t - F_{t-1}) + (1 - \beta)T_{t-1}$$

- $\beta \in [0, 1]$ is a trend weighting parameter.
- Trend formula allows for changing trend throughout the data.

Adjusted Exponential Smoothing

11/ 14

- **Adjusted exponential smoothing:** exponential smoothing that is adjusted to incorporate information on a *long-term trend*.

$$AF_t = F_t + T_t$$

- AF_t is the adjusted exponential smoothing forecast.
- F_t is the regular exponential smoothing forecast.
- T_t is the latest estimate of the trend.
- Trend is computed by,

$$T_t = \beta(F_t - F_{t-1}) + (1 - \beta)T_{t-1}$$

- $\beta \in [0, 1]$ is a trend weighting parameter.
- Trend formula allows for changing trend throughout the data.

Adjusted Exponential Smoothing

11/ 14

- **Adjusted exponential smoothing:** exponential smoothing that is adjusted to incorporate information on a *long-term trend*.

$$AF_t = F_t + T_t$$

- AF_t is the adjusted exponential smoothing forecast.
 - F_t is the regular exponential smoothing forecast.
 - T_t is the latest estimate of the trend.
- Trend is computed by,

$$T_t = \beta(F_t - F_{t-1}) + (1 - \beta)T_{t-1}$$

- $\beta \in [0, 1]$ is a trend weighting parameter.
- Trend formula allows for changing trend throughout the data.

Adjusted Exponential Smoothing

11 / 14

- **Adjusted exponential smoothing:** exponential smoothing that is adjusted to incorporate information on a *long-term trend*.

$$AF_t = F_t + T_t$$

- AF_t is the adjusted exponential smoothing forecast.
 - F_t is the regular exponential smoothing forecast.
 - T_t is the latest estimate of the trend.
- Trend is computed by,

$$T_t = \beta(F_t - F_{t-1}) + (1 - \beta)T_{t-1}$$

- $\beta \in [0, 1]$ is a trend weighting parameter.
- Trend formula allows for changing trend throughout the data.

Adjusted Exponential Smoothing

11/ 14

- **Adjusted exponential smoothing:** exponential smoothing that is adjusted to incorporate information on a *long-term trend*.

$$AF_t = F_t + T_t$$

- AF_t is the adjusted exponential smoothing forecast.
 - F_t is the regular exponential smoothing forecast.
 - T_t is the latest estimate of the trend.
- Trend is computed by,

$$T_t = \beta(F_t - F_{t-1}) + (1 - \beta)T_{t-1}$$

- $\beta \in [0, 1]$ is a trend weighting parameter.
- Trend formula allows for changing trend throughout the data.

Adjusted Exponential Smoothing

11/ 14

- **Adjusted exponential smoothing:** exponential smoothing that is adjusted to incorporate information on a *long-term trend*.

$$AF_t = F_t + T_t$$

- AF_t is the adjusted exponential smoothing forecast.
 - F_t is the regular exponential smoothing forecast.
 - T_t is the latest estimate of the trend.
- Trend is computed by,

$$T_t = \beta(F_t - F_{t-1}) + (1 - \beta)T_{t-1}$$

- $\beta \in [0, 1]$ is a trend weighting parameter.
- Trend formula allows for changing trend throughout the data.

Seasonal Adjustment

12/ 14

- Previous methods capture information in recent movements, but not past seasonal fluctuations.
 - Example, we may realize that construction employment is always lowest in Jan, Feb, and March.
- **Seasonal factor:** percentage of a total year that occurs in a specific season:

$$S_k = \frac{D_k}{\sum D_k}$$

- D_k is the sum of all values occurring in season k , for all years considered.
- Use your favorite forecasting method, forecast *years* only.
- For each season, multiply annual forecast by the seasonal factor.

Seasonal Adjustment

12/ 14

- Previous methods capture information in recent movements, but not past seasonal fluctuations.
 - Example, we may realize that construction employment is always lowest in Jan, Feb, and March.
- **Seasonal factor:** percentage of a total year that occurs in a specific season:

$$S_k = \frac{D_k}{\sum D_k}$$

- D_k is the sum of all values occurring in season k , for all years considered.
- Use your favorite forecasting method, forecast *years* only.
- For each season, multiply annual forecast by the seasonal factor.

Seasonal Adjustment

12/ 14

- Previous methods capture information in recent movements, but not past seasonal fluctuations.
 - Example, we may realize that construction employment is always lowest in Jan, Feb, and March.
- **Seasonal factor:** percentage of a total year that occurs in a specific season:

$$S_k = \frac{D_k}{\sum D_k}$$

- D_k is the sum of all values occurring in season k , for all years considered.
- Use your favorite forecasting method, forecast *years* only.
- For each season, multiply annual forecast by the seasonal factor.

Seasonal Adjustment

- Previous methods capture information in recent movements, but not past seasonal fluctuations.
 - Example, we may realize that construction employment is always lowest in Jan, Feb, and March.
- **Seasonal factor:** percentage of a total year that occurs in a specific season:

$$S_k = \frac{D_k}{\sum D_k}$$

- D_k is the sum of all values occurring in season k , for all years considered.
- Use your favorite forecasting method, forecast *years* only.
- For each season, multiply annual forecast by the seasonal factor.

Seasonal Adjustment

- Previous methods capture information in recent movements, but not past seasonal fluctuations.
 - Example, we may realize that construction employment is always lowest in Jan, Feb, and March.
- **Seasonal factor:** percentage of a total year that occurs in a specific season:

$$S_k = \frac{D_k}{\sum D_k}$$

- D_k is the sum of all values occurring in season k , for all years considered.
- Use your favorite forecasting method, forecast *years* only.
- For each season, multiply annual forecast by the seasonal factor.

Seasonal Adjustment

- Previous methods capture information in recent movements, but not past seasonal fluctuations.
 - Example, we may realize that construction employment is always lowest in Jan, Feb, and March.
- **Seasonal factor:** percentage of a total year that occurs in a specific season:

$$S_k = \frac{D_k}{\sum D_k}$$

- D_k is the sum of all values occurring in season k , for all years considered.
- Use your favorite forecasting method, forecast *years* only.
- For each season, multiply annual forecast by the seasonal factor.

Seasonal Adjustment

- Previous methods capture information in recent movements, but not past seasonal fluctuations.
 - Example, we may realize that construction employment is always lowest in Jan, Feb, and March.
- **Seasonal factor:** percentage of a total year that occurs in a specific season:

$$S_k = \frac{D_k}{\sum D_k}$$

- D_k is the sum of all values occurring in season k , for all years considered.
- Use your favorite forecasting method, forecast *years* only.
- For each season, multiply annual forecast by the seasonal factor.

Forecast Accuracy

13/ 14

- Useful to compare forecasts from multiple techniques.
- **Mean absolute deviation (MAD):** average distance between the forecast value and the actual value.

$$MAD = \frac{1}{T} \sum_{t=1}^T \|x_t - F_t\|$$

- **Mean absolute percentage deviation:** measures the distance between the forecast and actual values as a percentage of the total values.

$$MAPD = \frac{\sum_{t=1}^T \|x_t - F_t\|}{\sum_{t=1}^T x_t}$$

Forecast Accuracy

13/ 14

- Useful to compare forecasts from multiple techniques.
- **Mean absolute deviation (MAD):** average distance between the forecast value and the actual value.

$$MAD = \frac{1}{T} \sum_{t=1}^T \|x_t - F_t\|$$

- **Mean absolute percentage deviation:** measures the distance between the forecast and actual values as a percentage of the total values.

$$MAPD = \frac{\sum_{t=1}^T \|x_t - F_t\|}{\sum_{t=1}^T x_t}$$

Forecast Accuracy

13/ 14

- Useful to compare forecasts from multiple techniques.
- **Mean absolute deviation (MAD):** average distance between the forecast value and the actual value.

$$MAD = \frac{1}{T} \sum_{t=1}^T \|x_t - F_t\|$$

- **Mean absolute percentage deviation:** measures the distance between the forecast and actual values as a percentage of the total values.

$$MAPD = \frac{\sum_{t=1}^T \|x_t - F_t\|}{\sum_{t=1}^T x_t}$$

Forecast Accuracy

13/ 14

- Useful to compare forecasts from multiple techniques.
- **Mean absolute deviation (MAD):** average distance between the forecast value and the actual value.

$$MAD = \frac{1}{T} \sum_{t=1}^T \|x_t - F_t\|$$

- **Mean absolute percentage deviation:** measures the distance between the forecast and actual values as a percentage of the total values.

$$MAPD = \frac{\sum_{t=1}^T \|x_t - F_t\|}{\sum_{t=1}^T x_t}$$

Forecast Accuracy

13/ 14

- Useful to compare forecasts from multiple techniques.
- **Mean absolute deviation (MAD):** average distance between the forecast value and the actual value.

$$MAD = \frac{1}{T} \sum_{t=1}^T \|x_t - F_t\|$$

- **Mean absolute percentage deviation:** measures the distance between the forecast and actual values as a percentage of the total values.

$$MAPD = \frac{\sum_{t=1}^T \|x_t - F_t\|}{\sum_{t=1}^T x_t}$$

Forecast Accuracy and Bias

14/ 14

- **Mean Squared Error (MSE):** instead of taking absolute value of differences, square them:

$$MSE = \frac{1}{T} \sum_{t=1}^T (x_t - F_t)^2$$

- Variance of forecasts (population formula):

$$VAR = \frac{1}{T} \sum_{t=1}^T (F_t - \bar{F}_t)^2$$

- **Bias:** when a forecast is persistently wrong, either in the positive direction or negative direction. $Bias = \sqrt{MSE - VAR}$
- **Root Mean Squared Error (RMSE) = \sqrt{MSE} .**

Forecast Accuracy and Bias

- **Mean Squared Error (MSE):** instead of taking absolute value of differences, square them:

$$MSE = \frac{1}{T} \sum_{t=1}^T (x_t - F_t)^2$$

- Variance of forecasts (population formula):

$$VAR = \frac{1}{T} \sum_{t=1}^T (F_t - \bar{F}_t)^2$$

- **Bias:** when a forecast is persistently wrong, either in the positive direction or negative direction. $Bias = \sqrt{MSE - VAR}$
- **Root Mean Squared Error (RMSE) = \sqrt{MSE} .**

Forecast Accuracy and Bias

14/ 14

- **Mean Squared Error (MSE):** instead of taking absolute value of differences, square them:

$$MSE = \frac{1}{T} \sum_{t=1}^T (x_t - F_t)^2$$

- Variance of forecasts (population formula):

$$VAR = \frac{1}{T} \sum_{t=1}^T (F_t - \bar{F}_t)^2$$

- **Bias:** when a forecast is persistently wrong, either in the positive direction or negative direction. $Bias = \sqrt{MSE - VAR}$
- **Root Mean Squared Error (RMSE) = \sqrt{MSE} .**

Forecast Accuracy and Bias

14/ 14

- **Mean Squared Error (MSE):** instead of taking absolute value of differences, square them:

$$MSE = \frac{1}{T} \sum_{t=1}^T (x_t - F_t)^2$$

- Variance of forecasts (population formula):

$$VAR = \frac{1}{T} \sum_{t=1}^T (F_t - \bar{F}_t)^2$$

- **Bias:** when a forecast is persistently wrong, either in the positive direction or negative direction. $Bias = \sqrt{MSE - VAR}$
- **Root Mean Squared Error (RMSE) = \sqrt{MSE} .**

Forecast Accuracy and Bias

14/ 14

- **Mean Squared Error (MSE):** instead of taking absolute value of differences, square them:

$$MSE = \frac{1}{T} \sum_{t=1}^T (x_t - F_t)^2$$

- Variance of forecasts (population formula):

$$VAR = \frac{1}{T} \sum_{t=1}^T (F_t - \bar{F}_t)^2$$

- **Bias:** when a forecast is persistently wrong, either in the positive direction or negative direction. $Bias = \sqrt{MSE - VAR}$
- **Root Mean Squared Error (RMSE)** = \sqrt{MSE} .

Forecast Accuracy and Bias

14/ 14

- **Mean Squared Error (MSE):** instead of taking absolute value of differences, square them:

$$MSE = \frac{1}{T} \sum_{t=1}^T (x_t - F_t)^2$$

- Variance of forecasts (population formula):

$$VAR = \frac{1}{T} \sum_{t=1}^T (F_t - \bar{F}_t)^2$$

- **Bias:** when a forecast is persistently wrong, either in the positive direction or negative direction. $Bias = \sqrt{MSE - VAR}$
- **Root Mean Squared Error (RMSE)** = \sqrt{MSE} .

Forecast Accuracy and Bias

- **Mean Squared Error (MSE):** instead of taking absolute value of differences, square them:

$$MSE = \frac{1}{T} \sum_{t=1}^T (x_t - F_t)^2$$

- Variance of forecasts (population formula):

$$VAR = \frac{1}{T} \sum_{t=1}^T (F_t - \bar{F}_t)^2$$

- **Bias:** when a forecast is persistently wrong, either in the positive direction or negative direction. $Bias = \sqrt{MSE - VAR}$
- **Root Mean Squared Error (RMSE) = \sqrt{MSE} .**