# Forecasting

# BUS 735: Business Decision Making and Research

# 1

## 1.1 Goals and Agenda

Goals and Agenda	
Learning Objective	Active Learning Activity
Learn how to identify regulari-	Lecture / Excel Example.
ties in time series data	
Learn popular univariate time	Lecture / Excel Example.
series forecasting methods	
Learn how to use regression	Lecture / Excel Example.
analysis for forecasting	
Practice what we learn.	In-class exercise.
More practice.	Read Chapter 15, Homework
	exercises.
Assess what we have learned	Quiz??

# 2 Time Series Analysis

# 2.1 Example Data

## Working with Example Data

- Dataset: Total number of Mining, Logging, and Construction employees (in thousands) in the La Crosse area (obtained from Bureau of Labor Statistics website, http://www.bls.gov).
- To plot the data, we need to convert it to a single column:
  - 1. First generate observation numbers 1 through 116
  - 2. Figure out what row the observation is in: =int((obs-1)/12)+1
  - 3. Figure out what column the observation is in: =mod((obs-1),12)+1
  - 4. Pick out the right observation: =offset([top\_corner],row,col)
- Create dates: 2000.0 through 2010.58.

## Graphing Example Data

- In Excel: Insert, Line, Line with markers.
- Right click on data, select Select Data.
- Remove all the nonsense there.
- Select Add.
- Type "Employment" in Series Name. Select data for Series Values.
- Click Edit under Horizontal Axis Values.
- Select dates.

# 2.2 Time Series Characteristics

## **Time Series Characteristics**

- **Trend:** gradual, long-term movement of the data in a positive or negative direction.
- **Cycle:** repetitive up-and-down movement of the data, each "cycle" need not be the same length or magnitude.
- Seasonal pattern: up-and-down movement of the data that can be predicted quite accurately by the time of the year.
- **Random variations:** movements in the data that are otherwise unpredictable.

## 2.3 Forecasting Time Series

## **Time Series Analysis**

- **Time series analysis:** use of statistical methods to uncover trend, cyclical patterns, and seasonal patterns; and using this information to forecast future outcomes for a variable.
- Univariate time series: using many observations of only the variable of interest to forecast that variable.
- Multivariate time series: using one or more related variables to help forecast variable of interest.
  - New housing sales may also help predict construction employment.
  - National price measures for costs of building materials may also help predict construction employment.
- BUS 735: Focus on univariate time series analysis.

# 3 Time Series Methods

# 3.1 Smoothing Methods

#### Moving Average

- Naïve forecast: Forecast for tomorrow is what happened today.
  - Often used to measure usefulness of other time series forecasts.
- Moving average: uses several recent values to forecast the next period's outcome.

$$MA_{t,q} = \frac{1}{q} \sum_{i=1}^{q} x_{t-i}$$

- $-x_t$  denotes the value of the variable at time t,
- $-MA_{t,q}$  denotes the Moving Average forecast for time t, using the most recent q periods.

#### Moving Average Properties

- Moving average lag length:
  - Longer lag lengths cause forecast to react more quickly/slowly to recent changes in the variable.
  - Longer lag lengths cause forecast to be more smooth/volatile.
- Performs (forecasting accuracy) best with data that has
  - No pronounced cyclical or seasonal variation.
  - No long-term trend.

#### Weighted Moving Average

• Weighted moving average: like a moving average, but larger weights are assigned to more recent observations.

$$WMA_{t,q} = \sum_{i=1}^{q} w_i x_{t-i}$$

 $-w_i$  is the weight given to the observation that occurred *i* periods ago.

$$-\sum_{i=1}^{q} w_i = 1$$

- Typically,  $w_i > w_{i+1}$ .

• More recent observations are viewed as more informative.

### **Exponential Smoothing**

• Exponential smoothing: Averaging method using all previous data, but puts weights larger weight on the more recent observations.

$$F_t = \alpha x_{t-1} + (1 - \alpha) F_{t-1}$$

- $F_t$  is the forecast for period t.
- $x_{t-1}$  is the value of the variable in the previous time period, t-1.
- Useful for capturing information on recent seasonal or cyclical patterns (but with a lag).
- $\alpha \in [0,1]$  is the smoothing parameter.
  - When  $\alpha$  is larger, more weight is given to most recent observations.

#### **Adjusted Exponential Smoothing**

• Adjusted exponential smoothing: exponential smoothing that is adjusted to incorporate information on a *long-term trend*.

$$AF_t = F_t + T_t$$

- $-AF_t$  is the adjusted exponential smoothing forecast.
- $-F_t$  is the regular exponential smoothing forecast.
- $-T_t$  is the latest estimate of the trend.
- Trend is computed by,

$$T_t = \beta (F_t - F_{t-1}) + (1 - \beta)T_{t-1}$$

 $-\beta \in [0,1]$  is a trend weighting parameter.

• Trend formula allows for changing trend throughout the data.

# 3.2 Regression Methods

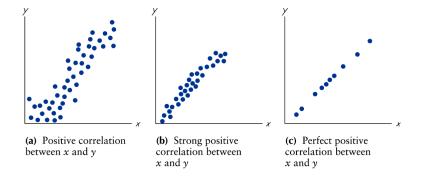
## Regression

- Regression line: equation of the line that describes the linear relationship between variable x and variable y.
- Need to assume that one variable causes another.
  - -x: independent or explanatory variable.
  - -y: dependent or outcome variable.
  - Variable x can influence the value for variable y, but not vice versa.

## **Regression Model Examples**

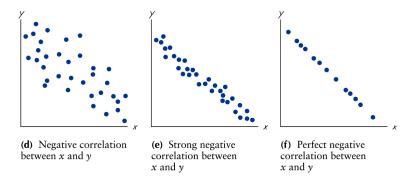
- How does housing demand affects construction employment?
  - $-x_i$ : housing demand (independent variable, aka explanatory variable).
  - $-y_i$ : construction employment (dependent variable, aka outcome variable).
- Seasonal adjustment: how does winter season affect construction employment?
  - Dummy variable:  $x_i = 1$  if winter,  $x_i = 0$  otherwise).
  - $y_i$ : construction employment.
- Be careful!
  - Construction demand
  - Construction worker pay

#### Positive linear correlation



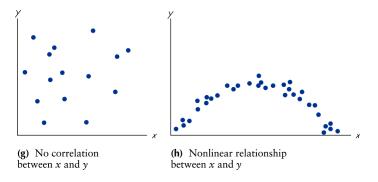
- Regression analysis will find equation for best fitting line for positively related variables.
- Stronger correlation, better forecast accuracy.
- Perfectly positively correlated??

#### Negative linear correlation



- Regression analysis will find equation for best fitting line for negatively related variables.
- Stronger correlation, better forecast accuracy.
- Perfectly negatively correlated??

#### No linear correlation



- Panel (g): no relationship at all.
- Panel (h): strong relationship, but not a *linear* relationship.
  - Need to transform your x variable before proceeding.

#### **Regression** line

• Population regression line:

$$y_i = \beta_0 + \beta_1 x_i + \epsilon_i$$

- The actual coefficients  $\beta_0$  and  $\beta_1$  describing the relationship between x and y are unknown.
- $-\epsilon_i$ : error term, since linear relationship between the x variables and y are not perfect.

• Use sample data to come up with an estimate of the regression line:

$$y_i = b_0 + b_1 x_i + e_i$$

 $-e_i$ : residual = the difference between the predicted value  $\hat{y}$  and the actual value  $y_i$ .

#### Interpreting the slope

- Interpreting the slope,  $b_1$ : amount the y is predicted to increase when increasing x by one unit.
- When  $b_1 < 0$  there is a negative linear relationship. That is increasing x causes y to decrease.
- When  $b_1 > 0$  there is a positive linear relationship. That is increasing x causes y to increase.
- When  $b_1 = 0$  there is no linear relationship between x and y.

#### Multiple Regression

• Multiple regression line (population):

$$y_i = \beta_0 + \beta_1 x_{1,i} + \beta_2 x_2 + \dots + \beta_{k-1} x_{k-1} + \epsilon_i$$

• Multiple regression line (sample):

$$y_i = b_0 + b_1 x_{1,i} + b_2 x_2 + \dots + b_k x_k + e_i$$

- -k+1: number of parameters (coefficients) you are estimating.
- Example, could use multiple variables to forecast construction employment:
  - New housing sales, measure of costs of construction materials, population growth.
  - Dummy for winter, Dummy for spring, Dummy for summer, time period (captures trend).

### Multicolinearity

- **Multicolinearity:** when two or more explanatory variables are closely related to one another.
- This makes distinguishing the causal effect of each variable difficult.
  - Example: using unemployment *and* consumer spending as explanatory variables for construction employment.

- When there is multicolinearity, one or more explanatory variables can accurately predict another explanatory variables.
  - Any one of these explanatory variables has little explanatory power over and above the others.
- Perfect multicolinearity: when one or more explanatory variables perfectly predicts another explanatory variables.
  - Regression analysis blows up.

# 3.3 Seasonal Adjustment

#### Seasonal Adjustment

- Previous methods capture information in recent movements, but not past seasonal fluctuations.
  - Example, we may realize that construction employment is always lowest in Jan, Feb, and March.
- Seasonal factor: percentage of a total year that occurs in a specific season:

$$S_k = \frac{D_k}{\sum D_k}$$

- $-D_k$  is the sum of all values occurring in season k, for all years considered.
- Use your favorite forecasting method, forecast *years* only.
- For each season, multiply annual forecast by the seasonal factor.

#### **Regression Seasonal Adjustment**

- Run a regression.
  - Use trend as an explanatory variable.
  - Use seasonal dummies as explanatory variables.
- Note: avoid multicolinearity, choose 1 fewer dummy variables than total seasons.
- Coefficient on seasonal dummies: impact of the season over and above excluded season dummy.

# 4 Forecast Accuracy

# 4.1 Absolute Deviations

### **Forecast Accuracy**

- Useful to compare forecasts from multiple techniques.
- Mean absolute deviation (MAD): average distance between the forecast value and the actual value.

$$MAD = \frac{1}{T} \sum_{t=1}^{T} \|x_t - F_t\|$$

• Mean absolute percentage deviation: measures the distance between the forecast and actual values as a percentage of the total values.

$$MAPD = \frac{\sum_{t=1}^{T} ||x_t - F_t||}{\sum_{t=1}^{T} x_t}$$

# 4.2 Squared Deviations and Bias

#### Forecast Accuracy and Bias

• Mean Squared Error (MSE): instead of taking absolute value of differences, square them:

$$MSE = \frac{1}{T} \sum_{t=1}^{T} (x_t - F_t)^2$$

• Variance of forecasts (population formula):

$$VAR = \frac{1}{T} \sum_{t=1}^{T} (F_t - \bar{F}_t)^2$$

- Bias: when a forecast is persistently wrong, either in the positive direction or negative direction. Bias =  $\sqrt{MSE VAR}$
- Root Mean Squared Error (RMSE) =  $\sqrt{MSE}$ .