Risk and Term Structure of Interest Rates

ECO 301: Money and Banking

Goals and Learning Outcomes

- Goals:
 - Explain factors that can cause interest rates to be different for bonds of different risk, liquidity, and maturity.
- Learning Outcomes:
 - LO3: Predict changes in interest rates using fundamental economic theories including present value calculations, behavior towards risk, and supply and demand models of money and bond markets.

Reading and Exercises

- Risk structure: Chapter 5, pp. 140-145
- Liquidity and taxes: Chapter 5, pp. 148-151
- Term Structure: Chapter 5, pp. 153-165
- Canvas quiz due Wed 11:59 PM.
- Homework/Exercise due Fri 11:59 PM. We will work together in class on Thursday

Risk Structure

- Risk structure of interest rates: explanation for why different securities with the same maturity have different prevailing interest rates in secondary market.
- Examples:
 - Federal government bonds.
 - Municipal bonds.
 - Aaa corporate bonds.
 - Baa corporate bonds.
- "Risk" structure actually includes multiple factors:
 - Default risk
 - Capital gains risk
 - Differences in liquidity
 - Differences in tax rules

Default Risk

- **Risk-free bonds** aka **default-free bonds**: bonds that have zero chance of default. Treasury bonds are often considered risk-free bonds.
- Default risk premium: additional interest above risk-free bonds paid for securities with a risk of default.
- Use a supply/demand analysis for two securities: Treasury bonds and Baa corporate bonds
- Higher risk of default → higher risk premium.

Credit Rating Agencies

- Three major credit rating agencies determine risk of default for many corporate and government bonds.
 - Moody's Investor Service
 - Standard and Poor's Corporation
 - Fitch Ratings
- "Investment-grade" securities have ratings Baa/BBB or above.
- "Junk bonds" or "high-yield" bonds have ratings below Baa/BBB.

Credit Rating Agencies

Moody's	S&P and Fitch	Definition
Aaa	AAA	Prime Maximum Safety
Aa1, Aa2, Aa3	AA+, AA, AA-	High Grade High Quality
A1, A2, A3	A+, A, A-	Upper Medium Grade
Baa1, Baa2, Baa3	BBB+, BBB, BBB-	Lower Medium Grade
Ba1, Ba2, Ba3	BB+, BB, BB-	Speculative
B1, B2, B3	B+, B, B-	Highly Speculative
Caa1, Caa2, Caa3	CCC+, CCC, CCC-	Extremely Speculative

Liquidity

- Bonds that differ on risk, usually also differ on liquidity.
- Treasury bonds are most highly liquid traded worldwide.
- For a given corporation, far fewer bonds are traded, many financial investors may not be familiar with security.
- Credit rating agencies help increase liquidity.
- Supply and demand analysis of Treasury bonds vs. corporate bonds again demonstrates premium paid for liquidity.
- What is called "risk structure" of interest rates: more appropriately should be called risk and liquidity structure.

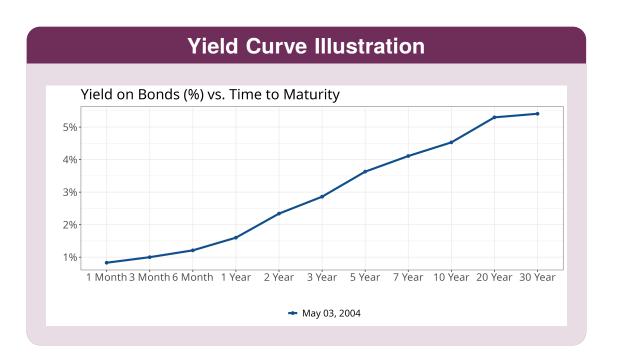
Municipal Bonds and Income Tax

- Municipal bonds have higher risk, lower liquidity than Treasury bonds.
- Yet, municipal bonds often have lower interest rates than risk-free Treasury bonds.
- Earnings on holding municipal bonds are exempt from Federal income taxes.
- Example consider two hypothetical, one year maturity, discount bonds:
 - Treasury bond: Face value = \$1000, Price = \$952.
 - Municipal bond: Face value = \$1000, Price = \$957.
 - Suppose tax rate = 15%
 - Compute before-tax and after-tax yield to maturity.
- Supply and demand analysis of Treasury bonds vs. municipal bonds demonstrates effect on interest rates.

Yield Curve

Time to Maturity

- Bonds with otherwise identical risk, liquidity and tax rules may have different interest rates due to different times remaining to maturity.
- Yield curve: illustration of how interest rates for a particular type of bond differ for different maturity dates.



Yield Curve

- Yield curve shape:
 - Yield curves are often, but not always, upward sloping.
 - Inverted yield curve: downward sloping.
 - Sometimes have more complicated shape.
- Theories that explain shape:
 - Expectations theory.
 - Liquidity theory.
- U.S. Treasury Yield Curve

Expectations Theory

- Bonds with different maturity dates, but otherwise similar features, should be nearly perfect substitutes to one another. → Consequently, returns to should be the same when held for the same period of time.
- Simple example: compare return of one-year security (rolled over for a second year) and a two-year security.
 - Let i_t denote today's (time t) interest rate for a one-year security.
 - Let $E_t i_{t+1}$ denote today's (time t) expectation of tomorrow's (time t+1 interest rate) on a one-year security.
 - Let $i_{2,t}$ denote the annual interest rate negotiated today (t) for the two-year bond.

Expectations Theory

• Expected two-year total return on holding one-year securities:

$$E_t R_1 = (1 + i_t)(1 + E_t i_{t+1}) - 1$$

= $i_t + E_t i_{t+1} + i_t E_t i_{t+1}$
 $\approx i_t + E_t i_{t+1}$

Expected two-year total return on holding two-year security:

$$R_2 = (1 + i_{2,t})(1 + i_{2,t}) - 1$$

= $2i_{2,t} + i_{2,t}^2$
 $\approx 2i_{2,t}$

• Perfect substitutes - set returns equal to another:

$$E_t R_1 = R_2$$
 $i_{2,t} = \frac{i_t + E_t i_{t+1}}{2}$

 Return on long-term bond is approximately equal to average expected interest rates until maturity date.

Expectations Theory

- Based on the expectations theory, when should yield curve be...
 - upward sloping?
 - downward sloping?
 - flat?
- Yield curves are almost always upward sloping. What explains that?

Liquidity Theory

- Long term bonds are subject to interest rate risk.
 - Holders of long-term bonds seldom plan to hold security.
 - Even if they did, higher interest rates in the future increase the opportunity cost of holding the bond.
- Liquidity theory: short-term and long-term bonds are close, but not perfect substitutes.
- In addition to paying interest equal to the average expected interest rate, bond issuers must pay a **liquidity premium**.
- The further is the maturity date, the larger is the interest rate risk, the larger is the liquidity premium.
- Suppose the current interest rate is equal to the long-run average expected interest rate. What should be the shape of the yield curve under expectations theory and liquidity theory?
- Under usual conditions, yield curves tend to be upward sloping.

Recessions and Yield Curves

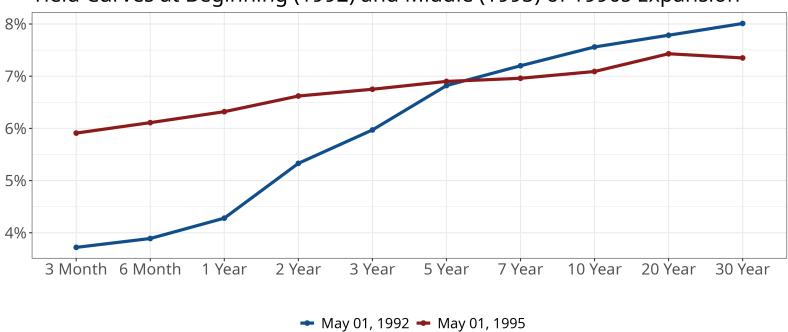
- Suppose people expect the economy may go into a recession.
- If that did happen, consider the following:
 - What would be the impact on businesses' decisions for making long-term capital investments? Describe and illustrate the impact on the market for long-term bonds. What happens to long-term interest rates?
 - How would the central bank react in order to stimulate the economy? What would happen to bond prices in this case? What happens to today's demand for long-term bonds based on this expectation?
- What might be the shape of the yield curve?
- Recessions tend to be preceded by yield curves that are flat or "inverted"

Healthy Economies and Yield Curves

- Suppose unemployment is low, real GDP is near potential GDP, inflation is low.
- Suppose default risk is low, people have confidence in bond ratings, high volume of trade in bonds.
- Suppose people expect the central bank to keep interest rates where they are.
- What would the expectations' theory suggest about the slope of the yield curve?
- What would the liquidity theory suggest about the slope of the yield curve?

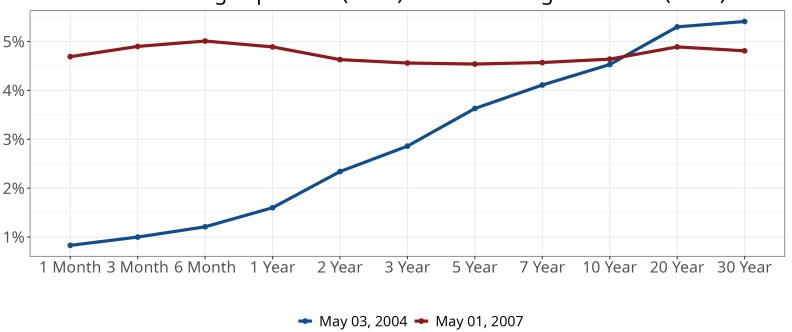
Yield Curve in Healthy Economy of 1990s





Yield Curve Preceding 2008-2009 Recession





Today's Yield Curve





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